## Ch 18 Confidence Intervals for Proportions Reference Sheet

Confidence Interval: A level C (usually 90, 95, or 99\%) confidence interval for a model parameter is a range of values usually of the form --- estimate $\pm$ margin of error ( $\mathbf{p} \pm \mathbf{M E}$ ) --- to show $\mathrm{C} \%$ of all random sample will yield intervals that capture the true parameter value ( $p$ ).

## Check for Assumptions and Conditions for finding and interpreting confidence intervals

1) Independence Assumption: sampled values are independent from each other.
2) Randomization Condition: must be random sample
3) $10 \%$ Condition: When not independent, the sample should be no more than $10 \%$ of the population
4) Success/Failure Condition: expect at least 10 successes and failures

Purpose: to draw conclusions and analyze outcomes by predicting the range of values most random samples will fall within.

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p= parameter of success
q= parameter of failure
n= sample size
z = critical value (z score) corresponding to confidence level
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Critical Value (z*): the number of standard errors (estimated deviations) to move away from the sample statistic (p) to specify the interval for a specified confidence level.

Components of Confidence Intervals (also known as One-Proportion z-Interval)

| Component | Description | Formula |
| :---: | :---: | :---: |
| Standard Error (SE) (same as SD) | Estimate of the standard deviation (spread) | $S E(\hat{p})=\sqrt{\frac{\hat{p} \hat{q}}{n}}$ |
| Margin of Error (ME) | Extent of the interval on either side of the $p$ value. <br> Product of critical value and standard error (SD estimate) | $M E=z^{*} \sqrt{\frac{\hat{p} \hat{q}}{n}}$ |
| One-Proportion z-interval | Confidence interval | $\hat{p} \pm z^{*} S E(\hat{p})$ |
| Calculator: 1-PropZint STAT>TESTS>1-PropZint $\mathrm{x}=$ \# of successes $\mathrm{n}=$ sample size C-level = confidence level (\%) | Calculates confidence intervals | $\begin{aligned} & 1-\text { PropZInt } \\ & \times: 54 \\ & \text { n:104 } \\ & \text { C-Level: } 95 \\ & \text { Calculate } \end{aligned}$ |

## Tips:

- Error doesn't mean mistake; it means how much variability from the true value $p$.
- Write a confidence interval as a range in decimals (low end, high end)
- A confidence interval is always concluded with a formal statement with percentages for the range
- Work backwards for the sample size if given the ME
- ME of $5 \%$ or less is acceptable
- Confidence intervals want to "trap" the true value within the range
- Confidence intervals work with Normal Models and the 68-95-99.7 Rule


## Confidence Interval for 95\% (2 standard deviations, or 2SE)

"traps" 95\% of random samples within the range


## Confidence Interval for 99.7\% (3 standard deviations, or 3SE)

"traps" $99.7 \%$ of random samples within the range


## Example of multiple confidence intervals

Green Line = true value ( $p$ )
Each segment represents a confidence interval with an attempt to "trap" the true value, $p$, within its range.
Not all are successful, which is why we cannot assume 100\% confidence


